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## SMOOTHNESS AND APPROXIMATIVE COMPACTNESS IN ORLICZ FUNCTION SPACES

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**ABSTRACT.** Some criteria for approximative compactness of every weakly\* closed convex set of Orlicz function spaces equipped with the Luxemburg norm are given. Although, criteria for approximative compactness of Orlicz function spaces equipped with the Luxemburg norm were known, we can easily deduce them from our main results.

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